Homework 8<br>MATH 165 - Fall 2020

Tufts University, Department of Mathematics
Due: November 5, 2020

## 1. Book Questions

Grinstead and Snell: Section $6.3 \# 18 ; 7.1 \# 7 ; 7.2 \# 13, \# 20$

## 2. Supplemental Question (Expectation for Coupon Collector Problem)

Consider a collection of $n$ distinct coupons $\left\{x_{i}\right\}_{i=1}^{n}$. Let us draw them uniformly at random with replacement. Let $X_{n}$ be the random variable equal to the number of draws until all $n$ distinct coupons are selected.
(a) Compute $\mathbb{E}\left(X_{n}\right)$.
(b) Perform a numerical simulation across a range of $n$ values to show the scaling of $\mathbb{E}\left(X_{n}\right)$ as a function of $n$. Does it agree with your computation in (a)?

